

Single machine problems

- **maximal polynomially solvable:**

$1 prec; r_i C_{max}$	Lawler (1973)
$1 prec; p_i = p; r_i L_{max}$	Simons (1978)
$1 prec; r_i; pmtn L_{max}$	Blazewicz (1976), Baker et al. (1983)
$1 prec; p_i = p; r_i \sum C_i$	Simons (1983)
$1 prec; pmtn; p_i = p; r_i \sum C_i$	Baptiste et al. (2004)
$1 r_i; pmtn \sum C_i$	Baker (1974)
$1 p_i = p; r_i \sum w_i C_i$	Baptiste (2000)
$1 sp - graph \sum w_i C_i$	Lawler (1978)
$1 r_i; pmtn \sum U_i$	Lawler (1990)
$1 p_i = p; r_i \sum w_i U_i$	Baptiste (1999)
$1 pmtn; p_i = p; r_i \sum w_i U_i$	Baptiste (1999)
$1 p_i = p; r_i \sum T_i$	Baptiste (2000)
$1 pmtn; p_i = p; r_i \sum T_i$	Tian et al. (2006)
$1 p_i = 1; r_i \sum w_i T_i$	Assignment-problem

- **maximal pseudopolynomially solvable:**

$1 r_i; pmtn \sum w_i U_i$	Lawler (1990)
$1 \sum T_i$	Lawler (1977), Du & Leung (1990)

- **minimal NP-hard:**

* $1 r_i L_{max}$	Lenstra et al. (1977)
* $1 chains; r_i; pmtn \sum C_i$	Lenstra (-)
* $1 prec \sum C_i$	Lawler (1978), Lenstra & Rinnooy Kan (1978)
* $1 r_i \sum C_i$	Lenstra et al. (1977)
* $1 chains; p_i = 1; r_i \sum w_i C_i$	Lenstra & Rinnooy Kan (1980)
* $1 prec; p_i = 1 \sum w_i C_i$	Lawler (1978), Lenstra & Rinnooy Kan (1978)
* $1 r_i; pmtn \sum w_i C_i$	Labetoulle et al. (1984)
* $1 chains; p_i = 1 \sum U_i$	Lenstra & Rinnooy Kan (1980)
$1 \sum w_i U_i$	Lawler & Moore (1969), Karp (1972)
$1 \sum T_i$	Lawler (1977), Du & Leung (1990)
* $1 chains; p_i = 1 \sum T_i$	Leung & Young (1990)
* $1 \sum w_i T_i$	Lawler (1977), Lenstra et al. (1977)

- **minimal open:**

$1 pmtn; p_i = p; r_i \sum w_i C_i$
$1 p_i = p; r_i \sum w_i T_i$

- **maximal open:**

$1 p_i = p; r_i \sum w_i T_i$
$1 pmtn; p_i = p; r_i \sum w_i T_i$

Parallel machine problems without preemption

• maximal polynomially solvable:

$P p_i = p; outtree; r_i C_{max}$	Brucker et al. (1977)
$P p_i = p; tree C_{max}$	Hu (1961), Davida & Linton (1976)
$Q p_i = p; r_i C_{max}$	Assignment-problem
$Q2 p_i = p; chains C_{max}$	Brucker et al. (1999)
$P p_i = 1; chains; r_i L_{max}$	Dror et al. (1998), Baptiste et al. (2004)
$P p_i = p;intree L_{max}$	Brucker et al. (1977), Monma (1982)
$P2 p_i = p; prec L_{max}$	Garey & Johnson (1976)
$P2 p_i = 1; prec; r_i L_{max}$	Garey & Johnson (1977)
$P p_i = 1; outtree; r_i \sum C_i$	Brucker et al. (2002), Huo & Leung (2005)
$P p_i = p; outtree \sum C_i$	Hu (1961)
$P2 p_i = 1; prec; r_i \sum C_i$	Baptiste & Timkovsky (2004)
$P2 p_i = p; prec \sum C_i$	Coffman & Graham (1972)
$Pm p_i = p; tree \sum C_i$	Baptiste et al. (2004)
$Qm p_i = p; r_i \sum C_i$	Dessouky et al. (1990)
$R \sum C_i$	Horn (1973), Bruno et al. (1974)
$P p_i = p; r_i \sum w_i C_i$	Brucker & Kravchenko (2008)
$P p_i = 1; r_i \sum w_i U_i$	Networkflowproblem
$Pm p_i = p; r_i \sum w_i U_i$	Baptiste et al. (2004)
$Q p_i = p \sum w_i U_i$	Assignment-problem
$P p_i = p; r_i \sum T_i$	Brucker & Kravchenko (2005)
$P p_i = 1; r_i \sum w_i T_i$	Networkflowproblem
$Q p_i = p \sum w_i T_i$	Assignment-problem

• maximal pseudopolynomially solvable:

$Qm r_i C_{max}$	Lawler et al. (1989)
$Qm \sum w_i C_i$	Lawler et al. (1989)
$Qm \sum w_i U_i$	Lawler et al. (1989)

• minimal NP-hard:

$P2 C_{max}$	Lenstra et al. (1977)
* $P C_{max}$	Garey & Johnson (1978)
* $P p_i = 1;intree; r_i C_{max}$	Brucker et al. (1977)
* $P p_i = 1; prec C_{max}$	Ullman (1975)
* $P2 chains C_{max}$	Du et al. (1991)
* $Q p_i = p; chains C_{max}$	Kubiak (1988)
* $P p_i = 1; outtree L_{max}$	Brucker et al. (1977)
* $P p_i = 1;intree; r_i \sum C_i$	Lenstra (-)
* $P p_i = 1; prec \sum C_i$	Lenstra & Rinnooy Kan (1978)
* $P2 chains \sum C_i$	Du et al. (1991)
* $P2 r_i \sum C_i$	Single-machine problem
* $P2 \sum w_i C_i$	Bruno et al. (1974)
* $P \sum w_i C_i$	Lenstra (-)
* $P2 p_i = 1; chains \sum w_i C_i$	Timkovsky (2003)
* $P2 p_i = 1; chains \sum U_i$	Single-machine problem
* $P2 p_i = 1; chains \sum T_i$	Single-machine problem

• minimal open:

$P2 p_i = p;intree; r_i C_{max}$	$P2 p_i = p; chains; r_i L_{max}$	$Pm p_i = 1; prec \sum C_i$
$Pm p_i = 1;intree; r_i C_{max}$	$Pm p_i = 1; outtree L_{max}$	$Q p_i = p; r_i \sum C_i$
$Pm p_i = 1; prec C_{max}$	$Q2 p_i = p; chains L_{max}$	$Q2 p_i = p; chains \sum C_i$
$Q2 p_i = p; chains; r_i C_{max}$	$Q2 p_i = p; r_i L_{max}$	$Q2 p_i = p; r_i \sum w_i C_i$
$Q2 p_i = p;intree C_{max}$	$P p_i = 1;intree \sum C_i$	$P p_i = p; r_i \sum U_i$
$Q2 p_i = p; outtree C_{max}$	$P2 p_i = p; chains; r_i \sum C_i$	$P2 p_i = p; r_i \sum w_i T_i$
$Qm p_i = p; chains C_{max}$	$Pm p_i = 1;intree; r_i \sum C_i$	

• maximal open:

$P p_i = p; chains; r_i L_{max}$	$Q p_i = p; tree \sum C_i$	$Q p_i = p; r_i \sum w_i U_i$
$Qm p_i = p; prec; r_i L_{max}$	$Qm p_i = p; prec; r_i \sum C_i$	$Q p_i = p; r_i \sum w_i T_i$
$Q p_i = p; outtree; r_i \sum C_i$		

Parallel machine problems with preemption

- **maximal polynomially solvable:**

$P outtree; pmtn; r_i C_{max}$	Lawler (1982)
$P tree; pmtn C_{max}$	Muntz & Coffman (1970), Gonzalez & Johnson (1980)
$Q chains; pmtn C_{max}$	Horvath et al. (1977)
$P intree; pmtn L_{max}$	Lawler (1982)
$Q2 prec; pmtn; r_i L_{max}$	Lawler (1982)
$R pmtn; r_i L_{max}$	Lawler & Labetoulle (1978)
$P2 p_i = p; prec; pmtn \sum C_i$	Coffman et al. (2003)
$P2 p_i = p; outtree; pmtn; r_i \sum C_i$	Lushchakova (2006)
$P p_i = 1; outtree; pmtn; r_i \sum C_i$	Brucker et al. (2002), Huo & Leung (2005)
$P p_i = p; outtree; pmtn \sum C_i$	Brucker et al. (2002)
$Q p_i = p; pmtn; r_i \sum C_i$	Kravchenko & Werner (2009)
$Q pmtn \sum C_i$	Labetoulle et al. (1984)
$P p_i = p; pmtn \sum w_i C_i$	McNaughton (1959)
$Q p_i = p; pmtn \sum U_i$	Baptiste et al. (2004)
$Qm pmtn \sum U_i$	Lawler (1979), Lawler & Martel (1989)
$P p_i = 1; pmtn; r_i \sum w_i U_i$	Brucker et al. (2003)
$Pm p_i = p; pmtn \sum w_i U_i$	Baptiste (2000B)
$P p_i = p; pmtn \sum T_i$	Baptiste et al. (2004)
$P p_i = 1; pmtn; r_i \sum w_i T_i$	Baptiste (2002)

- **maximal pseudopolynomially solvable:**

$Pm pmtn \sum w_i C_i$	McNaughton (1959), Lawler et al. (1989)
$Qm pmtn \sum w_i U_i$	Lawler (1979), Lawler & Martel (1989)

- **minimal NP-hard:**

* $P intree; pmtn; r_i C_{max}$	Lenstra (-)
* $P p_i = 1; prec; pmtn C_{max}$	Ullman (1976)
* $R2 chains; pmtn C_{max}$	Lenstra (-)
* $P outtree; pmtn L_{max}$	Lenstra (-)
$P2 pmtn; r_i \sum C_i$	Du et al. (1990)
* $P pmtn; r_i \sum C_i$	Brucker & Kravchenko (2004)
* $P2 chains; pmtn \sum C_i$	Du et al. (1991)
* $R pmtn \sum C_i$	Sitters (2001)
$P2 pmtn \sum w_i C_i$	Bruno et al. (1974)
* $P p_i = p; pmtn; r_i \sum w_i C_i$	Leung & Young (1990A)
* $P pmtn \sum w_i C_i$	Lenstra (-)
* $P2 p_i = 1; chains; pmtn \sum w_i C_i$	Timkovsky (2003), Du et al. (1991)
* $P2 pmtn; r_i \sum w_i C_i$	Labetoulle et al. (1984)
$P pmtn \sum U_i$	Lawler (1983)
$P2 pmtn; r_i \sum U_i$	Du et al. (1992)
* $P2 p_i = 1; chains; pmtn \sum U_i$	Baptiste et al. (2004)
* $R pmtn \sum U_i$	Sitters (2001)
$P p_i = p; pmtn \sum w_i U_i$	Brucker & Kravchenko (1999)
$P2 pmtn \sum w_i U_i$	Single-machine problem

- **minimal open:**

$Pm p_i = 1; intree; pmtn; r_i C_{max}$	$P2 p_i = 1; intree; pmtn; r_i \sum C_i$	$P2 p_i = p; pmtn; r_i \sum U_i$
$Pm p_i = 1; prec; pmtn C_{max}$	$Pm p_i = p; chains; pmtn; r_i \sum C_i$	$R2 pmtn \sum U_i$
$Qm p_i = p; chains; pmtn; r_i C_{max}$	$Pm p_i = 1; intree; pmtn \sum C_i$	$Q2 p_i = p; pmtn \sum w_i U_i$
$Qm p_i = p; intree; pmtn C_{max}$	$Q2 p_i = p; chains; pmtn \sum C_i$	$P2 p_i = 1; chains; pmtn \sum T_i$
$Qm p_i = p; outtree; pmtn C_{max}$	$R2 pmtn \sum C_i$	$P2 p_i = p; pmtn; r_i \sum T_i$
$Pm p_i = 1; chains; pmtn; r_i L_{max}$	$P2 p_i = p; pmtn; r_i \sum w_i C_i$	$P2 pmtn \sum T_i$
$Pm p_i = 1; outtree; pmtn L_{max}$	$Q2 p_i = p; pmtn \sum w_i C_i$	$Q2 p_i = p; pmtn \sum T_i$
$Qm p_i = p; chains; pmtn L_{max}$		$P2 p_i = p; pmtn \sum w_i T_i$

- **maximal open:**

$Q outtree; pmtn; r_i C_{max}$	$Q p_i = p; prec; pmtn; r_i \sum C_i$	$Q pmtn \sum T_i$
$Q tree; pmtn C_{max}$	$Q p_i = p; pmtn; r_i \sum U_i$	$Qm p_i = p; prec; pmtn; r_i \sum T_i$
$Q chains; pmtn; r_i L_{max}$	$Rm pmtn \sum U_i$	$Rm pmtn \sum T_i$
$Q intree; pmtn L_{max}$	$Qm p_i = p; pmtn; r_i \sum w_i U_i$	$Q p_i = p; pmtn \sum w_i T_i$
$Qm prec; pmtn; r_i L_{max}$	$Q p_i = p; tree; pmtn; r_i \sum T_i$	$Qm p_i = p; pmtn; r_i \sum w_i T_i$

Open-shop problems without preemption

• maximal polynomially solvable:

$O p_{ij} = 1; tree C_{max}$	Braesel et al. (1994)
$O2 C_{max}$	Gonzalez & Sahni (1976)
$O p_{ij} = 1;intree L_{max}$	Brucker et al. (1993), Brucker (1998)
$O p_{ij} = 1;chains;r_i L_{max}$	Baptiste et al. (2004)
$O2 p_{ij} = 1;prec;r_i L_{max}$	Brucker et al. (1993), Brucker (1998)
$O p_{ij} = 1;outtree \sum C_i$	Braesel et al. (1995)
$O2 p_{ij} = 1;outtree;r_i \sum C_i$	Lushchakova (2006)
$O2 p_{ij} = 1;prec \sum C_i$	Coffman et al. (2003)
$O p_{ij} = 1;r_i \sum C_i$	Brucker & Kravchenko (2004)
$O p_{ij} = 1 \sum w_i C_i$	Brucker et al. (1993)
$O p_{ij} = 1 \sum U_i$	Liu & Bulfin (1988)
$Om p_{ij} = 1;r_i \sum w_i U_i$	Baptiste (2003)
$O p_{ij} = 1 \sum T_i$	Liu & Bulfin (1988)

• minimal NP-hard:

$O3 C_{max}$	Gonzalez & Sahni (1976)
* $O C_{max}$	Lenstra (-)
* $O p_{ij} = 1;outtree;r_i C_{max}$	Timkovsky (2003)
* $O p_{ij} = 1;prec C_{max}$	Timkovsky (2003)
* $O2 chains C_{max}$	Tanaev et al. (1994)
* $O2 r_i C_{max}$	Lawler et al. (1981,1982)
* $O p_{ij} = 1;outtree L_{max}$	Timkovsky (2003)
* $O2 L_{max}$	Lawler et al. (1981,1982)
* $O2 \sum C_i$	Achugbue & Chin (1982)
* $O2 p_{ij} = 1;chains \sum w_i C_i$	Timkovsky (2003)
* $O3 p_{ij} = 1;chains \sum w_i C_i$	Timkovsky (2003)
* $O p_{ij} = 1;r_i \sum U_i$	Kravchenko (1999)
* $O2 p_{ij} = 1;chains \sum U_i$	Timkovsky (2003)
* $O3 p_{ij} = 1;chains \sum U_i$	Timkovsky (2003)
* $O2 p_{ij} = 1;chains \sum T_i$	Timkovsky (2003)
* $O3 p_{ij} = 1;chains \sum T_i$	Timkovsky (2003)

• minimal open:

$O3 p_{ij} = 1;intree;r_i C_{max}$	$O3 p_{ij} = 1;chains;r_i \sum C_i$	$O2 p_{ij} = 1;r_i \sum T_i$
$O3 p_{ij} = 1;outtree;r_i C_{max}$	$O3 p_{ij} = 1;intree \sum C_i$	$O3 p_{ij} = 1;r_i \sum T_i$
$O3 p_{ij} = 1;prec C_{max}$	$O2 p_{ij} = 1;r_i \sum w_i C_i$	$O2 p_{ij} = 1 \sum w_i T_i$
$O3 p_{ij} = 1;outtree L_{max}$	$O3 p_{ij} = 1;r_i \sum w_i C_i$	$O3 p_{ij} = 1 \sum w_i T_i$
$O2 p_{ij} = 1;intree;r_i \sum C_i$	$O p_{ij} = 1 \sum w_i U_i$	

• maximal open:

$O p_{ij} = 1;intree;r_i L_{max}$	$O p_{ij} = 1;prec;r_i \sum C_i$	$O p_{ij} = 1;r_i \sum w_i T_i$
$Om p_{ij} = 1;prec;r_i L_{max}$	$O p_{ij} = 1 \sum w_i U_i$	

Open-shop problems with preemption

- maximal polynomially solvable:

$O|pmtn;r_i|L_{max}$ Cho & Sahni (1981)

- minimal NP-hard:

* $O2|chains;pmtn|C_{max}$ Lenstra (-)
* $O2|pmtn|\sum C_i$ Du & Leung (1993)
* $O2|chains;pmtn|\sum C_i$ Lenstra (-)
* $O2|pmtn;r_i|\sum C_i$ Sriskandarajah & Wagneur (1994)
* $O3|pmtn|\sum C_i$ Liu & Bulfin (1985)
* $O2|pmtn|\sum w_i C_i$ Lenstra (-)
* $O2|pmtn|\sum U_i$ Lawler et al. (1981,1982)

Flow-shop problems without preemption

- **maximal polynomially solvable:**

$F p_{ij} = 1; outtree; r_i C_{max}$	Bruno et al. (1980)
$F p_{ij} = 1; tree C_{max}$	Bruno et al. (1980)
$F2 C_{max}$	Johnson (1954)
$F p_{ij} = 1;intree L_{max}$	Bruno et al. (1980)
$F2 p_{ij} = 1; prec; r_i L_{max}$	Bruno et al. (1980)
$F p_{ij} = 1; outtree; r_i \sum C_i$	Brucker & Knust (1999)
$F2 p_{ij} = 1; prec; r_i \sum C_i$	Baptiste & Timkovsky (2004)
$Fm p_{ij} = 1;intree \sum C_i$	Averbakh et al. (2005)
$F p_{ij} = 1; r_i \sum w_i U_i$	Single-machine problem
$F p_{ij} = 1; r_i \sum w_i T_i$	Single-machine problem

- **minimal NP-hard:**

* $F p_{ij} = 1;intree; r_i C_{max}$	Brucker & Knust (1999)
* $F p_{ij} = 1; prec C_{max}$	Leung et al. (1984), Timkovsky (2003)
* $F2 chains C_{max}$	Lenstra et al. (1977)
* $F2 r_i C_{max}$	Lenstra et al. (1977)
* $F3 C_{max}$	Garey et al. (1976)
* $F p_{ij} = 1; outtree L_{max}$	Brucker & Knust (1999)
* $F2 L_{max}$	Lenstra et al. (1977)
* $F2 \sum C_i$	Garey et al. (1976)
* $F2 p_{ij} = 1; chains \sum w_i C_i$	Tanaev et al. (1994)
* $F3 p_{ij} = 1; chains \sum w_i C_i$	Tanaev et al. (1994)
* $F2 p_{ij} = 1; chains \sum U_i$	Brucker & Knust (1999)
* $F3 p_{ij} = 1; chains \sum U_i$	Brucker & Knust (1999)
* $F2 p_{ij} = 1; chains \sum T_i$	Brucker & Knust (1999)
* $F3 p_{ij} = 1; chains \sum T_i$	Brucker & Knust (1999)

- **minimal open:**

$F3 p_{ij} = 1;intree; r_i C_{max}$	$F3 p_{ij} = 1; chains; r_i L_{max}$	$F p_{ij} = 1;intree \sum C_i$
$F3 p_{ij} = 1; prec C_{max}$	$F3 p_{ij} = 1; outtree L_{max}$	$F3 p_{ij} = 1;intree; r_i \sum C_i$
		$F3 p_{ij} = 1; tree \sum C_i$

- **maximal open:**

$F p_{ij} = 1; chains; r_i L_{max}$	$Fm p_{ij} = 1; prec; r_i L_{max}$	$F p_{ij} = 1; prec; r_i \sum C_i$
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Flow-shop problems with preemption

- **maximal polynomially solvable:**

$F2|pmtn|C_{max}$ Gonzalez & Sahni (1978), Cho & Sahni (1981)

- **minimal NP-hard:**

- * $F2|chains;pmtn|C_{max}$ Lenstra (-)
- * $F2|r_i;pmtn|C_{max}$ Gonzalez & Sahni (1978), Cho & Sahni (1981)
- * $F3|pmtn|C_{max}$ Gonzalez & Sahni (1978), Cho & Sahni (1981)
- * $F2|pmtn|L_{max}$ Gonzalez & Sahni (1978), Cho & Sahni (1981)
- * $F2|pmtn|\sum C_i$ Du & Leung (1993)

Job-shop problems without preemption

- **maximal polynomially solvable:**

$J2 p_{ij} = 1; r_i C_{max}$	Timkovsky (1997)
$J2 p_{ij} = 1 \sum C_i$	Kubiak & Timkovsky (1996)
$J2 p_{ij} = 1 \sum U_i$	Kravchenko (1999A)
$J prec; p_{ij} = 1; r_i; n = k \sum w_i U_i$	Brucker & Kraemer (1996)
$J prec; r_i; n = 2 \sum w_i U_i$	Sotskov (1991)
$J2 n = k \sum w_i U_i$	Brucker et al. (1997A)
$J prec; p_{ij} = 1; r_i; n = k \sum w_i T_i$	Brucker & Kraemer (1996)
$J prec; r_i; n = 2 \sum w_i T_i$	Sotskov (1991)
$J2 n = k \sum w_i T_i$	Brucker et al. (1997A)

- **maximal pseudopolynomially solvable:**

$J prec; r_i; n = k \sum w_i U_i$	Middendorf & Timkovsky (1999)
$J2 p_{ij} = 1 \sum w_i U_i$	Kravchenko (1999A)
$J prec; r_i; n = k \sum w_i T_i$	Middendorf & Timkovsky (1999)

- **minimal NP-hard:**

$J3 n = 3 C_{max}$	Sotskov & Shakhlevich (1995)
* $J2 C_{max}$	Lenstra & Rinnooy Kan (1979)
* $J2 chains; p_{ij} = 1 C_{max}$	Timkovsky (1985)
* $J3 p_{ij} = 1 C_{max}$	Lenstra & Rinnooy Kan (1979)
$J2 p_{ij} = 1; r_i \sum C_i$	Timkovsky (1998)
$J3 n = 3 \sum C_i$	Sotskov & Shakhlevich (1995)
* $J2 \sum C_i$	Garey et al. (1976)
* $J2 chains; p_{ij} = 1 \sum C_i$	Timkovsky (1998)
* $J3 p_{ij} = 1 \sum C_i$	Lenstra (-)
$J2 p_{ij} = 1 \sum w_i C_i$	Timkovsky (1998)
* $J2 p_{ij} = 1; r_i \sum w_i C_i$	Timkovsky (1998)
$J2 p_{ij} = 1; r_i \sum U_i$	Timkovsky (1998)
$J2 p_{ij} = 1 \sum w_i U_i$	Kravchenko (1999A)
* $J2 p_{ij} = 1 \sum w_i T_i$	Timkovsky (1998)

- **minimal open:**

$J2 chains; n = 3 C_{max}$	$J2 chains; n = 3 \sum C_i$	$J2 p_{ij} = 1; r_i L_{max}$
$J2 r_i; n = 3 C_{max}$	$J2 r_i; n = 3 \sum C_i$	$J2 p_{ij} = 1 \sum T_i$

- **maximal open:**

$J2 p_{ij} = 1; r_i L_{max}$	$J2 p_{ij} = 1 \sum T_i$	$J2 prec; r_i; n = k \sum w_i T_i$
$J2 prec; r_i; n = k \sum w_i U_i$		

Job-shop problems with preemption

- **maximal polynomially solvable:**

$J|prec;r_i;n=2;pmtn|\sum w_iU_i$ Sotskov (1991)

$J|prec;r_i;n=2;pmtn|\sum w_iT_i$ Sotskov (1991)

- **maximal pseudopolynomially solvable:**

$J|prec;r_i;n=k;pmtn|\sum w_iU_i$ Middendorf & Timkovsky (1999)

$J|prec;r_i;n=k;pmtn|\sum w_iT_i$ Middendorf & Timkovsky (1999)

- **minimal NP-hard:**

$J2|n=3;pmtn|C_{max}$ Brucker et al. (1999B)

* $J2|pmtn|C_{max}$ Lenstra & Rinnooy Kan (1979)

$J2|n=3;pmtn|\sum C_i$ Brucker et al. (1999B)

* $J2|pmtn|\sum C_i$ Lenstra (-)

Open-shop problems with no wait

• maximal polynomially solvable:

$O p_{ij} = 1; tree; no - wait C_{max}$	Brucker et al. (1993), Hu (1961)
$O2 p_{ij} = 1; chains; r_i; no - wait C_{max}$	Timkovsky (2003)
$O2 p_{ij} = 1; prec; no - wait C_{max}$	Brucker et al. (1993), Coffman & Graham (1972)
$O p_{ij} = 1;intree; no - wait L_{max}$	Brucker et al. (1993), Brucker et al. (1977)
$O p_{ij} = 1; r_i; no - wait L_{max}$	Brucker et al. (1993), Simons (1983)
$O p_{ij} = 1; outtree; no - wait \sum C_i$	Brucker et al. (1993), Hu (1961)
$O p_{ij} = 1; r_i; no - wait \sum C_i$	Timkovsky (2003)
$O2 p_{ij} = 1; chains; r_i; no - wait \sum C_i$	Timkovsky (2003)
$O2 p_{ij} = 1; prec; no - wait \sum C_i$	Timkovsky (2003)
$Om p_{ij} = 1;intree; no - wait \sum C_i$	Baptiste et al. (2004)
$Om p_{ij} = 1; r_i; no - wait \sum w_i C_i$	Timkovsky (2003)
$O p_{ij} = 1; no - wait \sum w_i U_i$	Kubiak et al. (1991)
$Om p_{ij} = 1; r_i; no - wait \sum w_i U_i$	Baptiste et al. (2004)
$Om p_{ij} = 1; r_i; no - wait \sum T_i$	Timkovsky (2003)
$O p_{ij} = 1; no - wait \sum w_i T_i$	Brucker et al. (1993)

• minimal NP-hard:

* $O p_{ij} = 1; prec; no - wait C_{max}$	Ullman (1975)
* $O2 no - wait C_{max}$	Sahni & Cho (1979)
* $O p_{ij} = 1; outtree; no - wait L_{max}$	Brucker et al. (1977)
* $O p_{ij} = 1; prec; no - wait \sum C_i$	Lenstra & Rinnooy Kan (1978)
* $O2 no - wait \sum C_i$	Kubiak et al. (1991)
* $O2 p_{ij} = 1; chains; no - wait \sum w_i C_i$	Timkovsky (2003)
* $O3 p_{ij} = 1; chains; no - wait \sum w_i C_i$	Timkovsky (2003)
* $O2 p_{ij} = 1; chains; no - wait \sum U_i$	Timkovsky (2003)
* $O3 p_{ij} = 1; chains; no - wait \sum U_i$	Timkovsky (2003)
* $O2 p_{ij} = 1; chains; no - wait \sum T_i$	Timkovsky (2003)
* $O3 p_{ij} = 1; chains; no - wait \sum T_i$	Timkovsky (2003)

• minimal open:

$O2 p_{ij} = 1;intree; r_i; no - wait C_{max}$	$O3 p_{ij} = 1; chains; r_i; no - wait \sum C_i$
$O2 p_{ij} = 1; outtree; r_i; no - wait C_{max}$	$O3 p_{ij} = 1; tree; no - wait \sum C_i$
$O3 p_{ij} = 1; chains; r_i; no - wait C_{max}$	$O p_{ij} = 1;intree; no - wait \sum C_i$
$O3 p_{ij} = 1; prec; no - wait C_{max}$	$O p_{ij} = 1; r_i; no - wait \sum w_i C_i$
$O2 p_{ij} = 1; chains; r_i; no - wait L_{max}$	$O p_{ij} = 1; r_i; no - wait \sum U_i$
$O2 p_{ij} = 1; outtree; no - wait L_{max}$	$O p_{ij} = 1; r_i; no - wait \sum T_i$
$O3 p_{ij} = 1; outtree; no - wait L_{max}$	$O2 p_{ij} = 1; r_i; no - wait \sum w_i T_i$
$O2 p_{ij} = 1;intree; r_i; no - wait \sum C_i$	$O3 p_{ij} = 1; r_i; no - wait \sum w_i T_i$
$O2 p_{ij} = 1; outtree; r_i; no - wait \sum C_i$	

• maximal open:

$O p_{ij} = 1; tree; r_i; no - wait C_{max}$	$Om p_{ij} = 1; prec; r_i; no - wait \sum C_i$
$O p_{ij} = 1;intree; r_i; no - wait L_{max}$	$O p_{ij} = 1; r_i; no - wait \sum w_i U_i$
$Om p_{ij} = 1; prec; r_i; no - wait L_{max}$	$O p_{ij} = 1; r_i; no - wait \sum w_i T_i$
$O p_{ij} = 1; tree; r_i; no - wait \sum C_i$	

Flow-shop problems with no wait

- **maximal polynomially solvable:**

$F2|no - wait|C_{max}$ Gilmore & Gomory (1964), Reddi & Ramamoorthy (1972)

- **minimal NP-hard:**

- * $F2|r_i; no - wait|C_{max}$ Roeck (1984)
 - * $F3|no - wait|C_{max}$ Roeck (1984A)
 - * $F2|no - wait|L_{max}$ Roeck (1984)
 - * $F2|no - wait|\sum C_i$ Roeck (1984)
-

- **minimal open:**

$F2|chains; no - wait|C_{max}$

- **maximal open:**

$F2|prec; no - wait|C_{max}$

Job-shop problems with no wait

- **maximal polynomially solvable:**

$J2 p_{ij} = 1; no - wait \sum C_i$	Kravchenko (1998)
$J prec; r_i; n = k; no - wait \sum w_i U_i$	Baptiste et al. (2004)
$J prec; r_i; n = k; no - wait \sum w_i T_i$	Baptiste et al. (2004)

- **maximal pseudopolynomially solvable:**

$J2 p_{ij} = 1; no - wait C_{max}$	Timkovsky (1985), Kubiak (1989)
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- **minimal NP-hard:**

$J2 p_{ij} = 1; no - wait C_{max}$	Timkovsky (1985), Kubiak (1989)
* $J2 chains; p_{ij} = 1; no - wait C_{max}$	Timkovsky (1998)
* $J2 no - wait C_{max}$	Sahni & Cho (1979)
* $J3 p_{ij} = 1; no - wait C_{max}$	Sriskandarajah & Ladet (1986)
* $J2 p_{ij} = 1; r_i; no - wait L_{max}$	Timkovsky (1998)
* $J2 chains; p_{ij} = 1; no - wait \sum C_i$	Timkovsky (1998)
* $J2 no - wait \sum C_i$	Roeck (1984)
* $J2 p_{ij} = 1; r_i; no - wait \sum C_i$	Timkovsky (1998)
* $J3 p_{ij} = 1; no - wait \sum C_i$	Sriskandarajah & Ladet (1986)
$J2 p_{ij} = 1; no - wait \sum w_i C_i$	Timkovsky (1998)
* $J2 p_{ij} = 1; no - wait \sum w_i T_i$	Timkovsky (1998)

Multiprocessor task problems with dedicated processors

- **maximal polynomially solvable:**

$P2 fix_i C_{max}$	Hoogeveen et al. (1994)
$Pm r_i; p_i = 1; fix_i C_{max}$	Brucker & Kraemer (1996)
$Pm r_i; p_i = 1; fix_i \sum C_i$	Brucker & Kraemer (1996)
$Pm p_i = 1; fix_i \sum w_i C_i$	Brucker & Kraemer (1996)
$Pm p_i = 1; fix_i \sum w_i U_i$	Brucker & Kraemer (1996)
$Pm p_i = 1; fix_i \sum T_i$	Brucker & Kraemer (1996)

- **minimal NP-hard:**

* $P p_i = 1; fix_i C_{max}$	Hoogeveen et al. (1994)
* $P2 chains; p_i = 1; fix_i C_{max}$	Hoogeveen et al. (1994), Blazewicz et al. (1983)
* $P2 r_i; fix_i C_{max}$	Hoogeveen et al. (1994)
* $P3 fix_i C_{max}$	Blazewicz et al. (1992), Hoogeveen et al. (1994)
* $P2 fix_i L_{max}$	Hoogeveen et al. (1994)
* $P p_i = 1; fix_i \sum C_i$	Hoogeveen et al. (1994)
* $P2 fix_i \sum C_i$	Hoogeveen et al. (1994), Cai et al. (1998)
* $P2 chains; p_i = 1; fix_i \sum C_i$	Hoogeveen et al. (1994), Blazewicz et al. (1983)

- **minimal open:**

$P2 r_i; p_i = 1; fix_i L_{max}$
$P2 r_i; p_i = 1; fix_i \sum w_i C_i$
$P2 p_i = 1; fix_i \sum w_i T_i$

- **maximal open:**

$Pm r_i; p_i = 1; fix_i \sum w_i U_i$
$Pm r_i; p_i = 1; fix_i \sum w_i T_i$

Multiprocessor task problems with dedicated processors and preemption

- **maximal polynomially solvable:**

$Pm|r_i; pmtn; fix_i|L_{max}$ Bianco et al. (1997)

$P2|pmtn; fix_i|\sum C_i$ Cai et al. (1998)

- **maximal pseudopolynomially solvable:**

- **minimal NP-hard:**

* $P|pmtn; fix_i|C_{max}$ Hoogeveen et al. (1994), Kubale (1990)

* $P2|chains; pmtn; fix_i|C_{max}$ Hoogeveen et al. (1994)

* $P|pmtn; fix_i|\sum C_i$ Hoogeveen et al. (1994)

* $P2|chains; pmtn; fix_i|\sum C_i$ Hoogeveen et al. (1994)

* $P2|pmtn; fix_i|\sum w_i C_i$ Oguz & Qi (2006)

- **minimal open:**

$P2|r_i; pmtn; fix_i|\sum C_i$

$P3|pmtn; fix_i|\sum C_i$

$P2|pmtn; fix_i|\sum U_i$

$P2|pmtn; fix_i|\sum T_i$

- **maximal open:**

$Pm|r_i; pmtn; fix_i|\sum w_i U_i$

$Pm|r_i; pmtn; fix_i|\sum T_i$

Multiprocessor task problems with parallel processors

- **maximal polynomially solvable:**

$P outtree; r_i; p_i = p C_{max}$	Brucker et al. (1977)
$P tree; p_i = p C_{max}$	Hu (1961), Davida & Linton (1976)
$P2 prec; p_i = p; size_i C_{max}$	Lloyd (1981)
$Pm r_i; p_i = p; size_i C_{max}$	Baptiste (2003B)
$P chains; r_i; p_i = 1 L_{max}$	Dror et al. (1998), Baptiste et al. (2004)
$P intree; p_i = p L_{max}$	Brucker et al. (1977), Monma (1982)
$P2 prec; r_i; p_i = 1 L_{max}$	Garey & Johnson (1977)
$P \sum C_i$	Bruno et al. (1974)
$P outtree; p_i = p \sum C_i$	Hu (1961)
$P outtree; r_i; p_i = 1 \sum C_i$	Brucker et al. (2002)
$P2 prec; p_i = p \sum C_i$	Coffman & Graham (1972)
$Pm intree; p_i = p \sum C_i$	Baptiste et al. (2004)
$Pm r_i; p_i = p; size_i \sum C_i$	Baptiste (2003B)
$P r_i; p_i = p \sum w_i C_i$	Brucker & Kravchenko (2008)
$Pm p_i = p; size_i \sum w_i C_i$	Drozdowski & Dell' Olmo (2000)
$P2 r_i; p_i = 1; size_i L_{max}$	Baptiste & Schieber (2003)
$Pm r_i; p_i = p \sum w_i U_i$	Baptiste et al. (2004)
$Pm p_i = p; size_i \sum w_i U_i$	Brucker et al. (2000)
$P r_i; p_i = p \sum T_i$	Brucker & Kravchenko (2005)
$Pm p_i = p; size_i \sum T_i$	Brucker et al. (2000)
$P p_i = p \sum w_i U_i, \sum w_i T_i$	Assignment-problem
$P r_i; p_i = 1 \sum w_i U_i, \sum w_i T_i$	Networkflowproblem

- **maximal pseudopolynomially solvable:**

$P3 size_i C_{max}$	Du & Leung (1989)
$Pm r_i C_{max}, Pm \sum w_i C_i, Pm \sum w_i U_i$	Lawler et al. (1989)

- **minimal NP-hard:**

$P2 C_{max}$	Lenstra et al. (1977)
* $P C_{max}$	Garey & Johnson (1978)
* $P intree; r_i; p_i = 1 C_{max}$	Brucker et al. (1977)
* $P p_i = 1; size_i C_{max}$	Lloyd (1981)
* $P prec; p_i = 1 C_{max}$	Ullman (1975)
* $P2 chains C_{max}$	Du et al. (1991)
* $P2 chains; r_i; p_i = 1; size_i C_{max}$	Brucker et al. (2000)
* $P2 r_i; size_i C_{max}$	Lee & Cai (1999)
* $P3 chains; p_i = 1; size_i C_{max}$	Blazewicz & Liu (1996)
* $P5 size_i C_{max}$	Du & Leung (1989)
* $P outtree; p_i = 1 L_{max}$	Brucker et al. (1977)
* $P2 chains; p_i = 1; size_i L_{max}$	Brucker et al. (2000)
* $P2 size_i L_{max}$	Lee & Cai (1999)
$P2 size_i \sum C_i$	Lee & Cai (1999)
* $P intree; r_i; p_i = 1 \sum C_i$	Lenstra (-)
* $P p_i = 1; size_i \sum C_i$	Drozdowski & Dell' Olmo (2000)
* $P prec; p_i = 1 \sum C_i$	Lenstra & Rinnooy Kan (1978)
* $P2 chains \sum C_i$	Du et al. (1991)
* $P2 intree; p_i = 1; size_i \sum C_i$	Zinder & Do (2005)
* $P2 outtree; p_i = 1; size_i \sum C_i$	Zinder et al. (2005)
* $P2 r_i \sum C_i$	Single-machine problem
$P2 \sum w_i C_i$	Bruno et al. (1974)
* $P \sum w_i C_i$	Lenstra (-)
* $P2 chains; p_i = 1 \sum w_i C_i$	Timkovsky (1998)
* $P2 size_i \sum w_i C_i$	Lee & Cai (1999)
* $P2 chains; p_i = 1 \sum U_i, \sum T_i$	Single-machine problem

- **minimal open:**

$P2 r_i; p_i = p; size_i L_{max}$	$P2 r_i; p_i = 1; size_i \sum w_i C_i$	$P2 r_i; p_i = 1; size_i \sum T_i$
$Pm r_i; p_i = 1; size_i L_{max}$	$P2 r_i; p_i = 1; size_i \sum U_i$	$P2 p_i = 1; size_i \sum w_i T_i$
$P2 chains; p_i = 1; size_i \sum C_i$		

- **maximal open:**

$Pm chains; r_i; p_i = p; size_i \sum C_i$	$Pm r_i; p_i = p; size_i \sum w_i U_i$	$Pm r_i; p_i = p; size_i \sum w_i T_i$
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Multiprocessor task problems with parallel processors and preemption

- **maximal polynomially solvable:**

$P outtree; pmtn; r_i C_{max}$	Lawler (1982)
$P tree; pmtn C_{max}$	Muntz & Coffman (1970), Gonzalez & Johnson (1980)
$Q chains; pmtn C_{max}$	Horvath et al. (1977)
$P intree; pmtn L_{max}$	Lawler (1982)
$Pm pmtn; r_i; size_i L_{max}$	Blazewicz et al. (1996)
$Q2 prec; pmtn; r_i L_{max}$	Lawler (1982)
$R pmtn; r_i L_{max}$	Lawler & Labetoulle (1978)
$P2 p_i = p; prec; pmtn \sum C_i$	Coffman et al. (2003)
$P2 p_i = p; outtree; pmtn; r_i \sum C_i$	Lushchakova (2006)
$P p_i = p; pmtn; r_i \sum C_i$	Brucker & Kravchenko (2004)
$P p_i = 1; outtree; pmtn; r_i \sum C_i$	Brucker et al. (2002), Huo & Leung (2005)
$P p_i = p; outtree; pmtn \sum C_i$	Brucker et al. (2002)
$Q pmtn \sum C_i$	Labetoulle et al. (1984)
$P p_i = p; pmtn \sum w_i C_i$	McNaughton (1959)
$Q p_i = p; pmtn \sum U_i$	Baptiste et al. (2004)
$Qm pmtn \sum U_i$	Lawler (1979), Lawler & Martel (1989)
$P p_i = 1; pmtn; r_i \sum w_i U_i$	Brucker et al. (2003)
$Pm p_i = p; pmtn \sum w_i U_i$	Baptiste (2000B)
$P p_i = p; pmtn \sum T_i$	Baptiste et al. (2004)
$P p_i = 1; pmtn; r_i \sum w_i T_i$	Baptiste (2002)

- **maximal pseudopolynomially solvable:**

$Pm pmtn \sum w_i C_i$	McNaughton (1959), Lawler et al. (1989)
$Qm pmtn \sum w_i U_i$	Lawler (1979), Lawler & Martel (1989)

- **minimal NP-hard:**

$P p_i = 1; pmtn; size_i C_{max}$	Drozdowski (1992)
* $P intree; pmtn; r_i C_{max}$	Lenstra (-)
* $P p_i = 1; prec; pmtn C_{max}$	Ullman (1976)
* $R2 chains; pmtn C_{max}$	Lenstra (-)
* $P outtree; pmtn L_{max}$	Lenstra (-)
$P2 pmtn; r_i \sum C_i$	Du et al. (1990)
$P pmtn; size_i \sum C_i$	Drozdowski & Dell' Olmo (2000)
* $P pmtn; r_i \sum C_i$	Brucker & Kravchenko (2004)
* $P2 chains; pmtn \sum C_i$	Du et al. (1991)
* $R pmtn \sum C_i$	Sitters (2001)
$P2 pmtn \sum w_i C_i$	Bruno et al. (1974)
* $P p_i = p; pmtn; r_i \sum w_i C_i$	Leung & Young (1990A)
* $P pmtn \sum w_i C_i$	Lenstra (-)
* $P2 p_i = 1; chains; pmtn \sum w_i C_i$	Timkovsky (2003), Du et al. (1991)
* $P2 pmtn; r_i \sum w_i C_i$	Labetoulle et al. (1984)
$P pmtn \sum U_i$	Lawler (1983)
$P2 pmtn; r_i \sum U_i$	Du et al. (1992)
* $P2 p_i = 1; chains; pmtn \sum U_i$	Baptiste et al. (2004)
* $R pmtn \sum U_i$	Sitters (2001)
$P p_i = p; pmtn \sum w_i U_i$	Brucker & Kravchenko (1999)
$P2 pmtn \sum w_i U_i$	Single-machine problem

- **minimal open:**

$P2 p_i = 1; chains; pmtn; size_i C_{max}$	$P2 p_i = 1; pmtn; size_i \sum C_i$
$Q2 p_i = p; pmtn; size_i C_{max}$	$P2 p_i = 1; pmtn; size_i \sum U_i$

- **maximal open:**

$Qm prec; pmtn; r_i; size_i L_{max}$	$Rm pmtn; size_i \sum U_i$
$Rm pmtn; r_i; size_i L_{max}$	$Qm p_i = p; pmtn; r_i; size_i \sum w_i U_i$
$Q p_i = p; prec; pmtn; r_i; size_i \sum C_i$	$Qm p_i = p; prec; pmtn; r_i; size_i \sum T_i$
$P p_i = 1; pmtn; r_i; size_i \sum w_i C_i$	$Rm pmtn; size_i \sum T_i$
$Q p_i = p; pmtn; size_i \sum w_i C_i$	$Qm p_i = p; pmtn; r_i; size_i \sum w_i T_i$

Shop problems with multiprocessor tasks

- **maximal polynomially solvable:**

$FMPTm r_i; p_{ij} = 1 C_{max}$	Brucker & Kraemer (1996)
$FMPTm r_i; p_{ij} = 1 \sum C_i$	Brucker & Kraemer (1996)
$FMPTm p_{ij} = 1 \sum w_i C_i$	Brucker & Kraemer (1996)
$FMPTm p_{ij} = 1 \sum w_i U_i$	Brucker & Kraemer (1996)
$FMPTm prec; r_i; n = k \sum w_i U_i$	Kraemer (1995)
$FMPTm p_{ij} = 1 \sum T_i$	Brucker & Kraemer (1996)
$FMPTm prec; r_i; n = k \sum w_i T_i$	Kraemer (1995)
$JMPT2 n = k C_{max}$	Brucker & Kraemer (1995)
$JMPT n = 2 \sum w_i U_i$	Brucker (1995)
$JMPT prec; r_i; p_{ij} = 1; n = k \sum w_i U_i$	Brucker & Kraemer (1996)
$JMPT n = 2 \sum w_i T_i$	Brucker (1995)
$JMPT prec; r_i; p_{ij} = 1; n = k \sum w_i T_i$	Brucker & Kraemer (1996)
$OMPT2 C_{max}$	Brucker & Kraemer (1995)
$OMPTm r_i; p_{ij} = 1 C_{max}$	Brucker & Kraemer (1996)
$OMPTm r_i; p_{ij} = 1 \sum C_i$	Brucker & Kraemer (1996)
$OMPTm p_{ij} = 1 \sum w_i C_i$	Brucker & Kraemer (1996)
$OMPT prec; r_i; p_{ij} = 1; n = 2 \sum w_i U_i$	Kraemer (1995)
$OMPTm p_{ij} = 1 \sum w_i U_i$	Brucker & Kraemer (1996)
$OMPTm prec; r_i; n = k \sum w_i U_i$	Kraemer (1995)
$OMPTm p_{ij} = 1 \sum T_i$	Brucker & Kraemer (1996)
$OMPT prec; r_i; p_{ij} = 1; n = 2 \sum w_i T_i$	Kraemer (1995)
$OMPTm prec; r_i; n = k \sum w_i T_i$	Kraemer (1995)

- **minimal NP-hard:**

$FMPT n = 3 C_{max}$	Kraemer (1995)
* $FMPT prec; p_{ij} = 1 C_{max}$	Timkovsky (2003)
* $FMPT tree; r_i; p_{ij} = 1 C_{max}$	Brucker & Knust (1999)
* $FMPT2 C_{max}$	Brucker & Kraemer (1995)
* $FMPT tree; p_{ij} = 1 L_{max}$	Brucker & Knust (1999)
* $FMPT2 \sum C_i$	Garey et al. (1976)
* $FMPT2 chains; p_{ij} = 1 \sum w_i C_i$	Tanaev et al. (1994)
* $FMPT2 chains; p_{ij} = 1 \sum U_i$	Single-machine problem
* $FMPT2 chains; p_{ij} = 1 \sum T_i$	Single-machine problem
$JMPT3 n = 3 C_{max}$	Sotskov & Shakhlevich (1995)
* $JMPT2 p_{ij} = 1 C_{max}$	Brucker & Kraemer (1995)
$JMPT2 r_i; p_{ij} = 1 \sum C_i$	Timkovsky (1998)
$JMPT3 n = 3 \sum C_i$	Sotskov & Shakhlevich (1995)
* $JMPT2 chains; p_{ij} = 1 \sum C_i$	Timkovsky (1998)
* $JMPT3 p_{ij} = 1 \sum C_i$	Lenstra (-)
$JMPT2 p_{ij} = 1 \sum w_i C_i$	Timkovsky (1998)
* $JMPT2 r_i; p_{ij} = 1 \sum w_i C_i$	Timkovsky (1998)
$OMPT n = 3 C_{max}$	Gonzalez & Sahni (1976)
$OMPT3 C_{max}$	Gonzalez & Sahni (1976)
* $OMPT C_{max}$	Lenstra (-)
* $OMPT prec; p_{ij} = 1 C_{max}$	Timkovsky (2003)
* $OMPT tree; r_i; p_{ij} = 1 C_{max}$	Timkovsky (2003)
* $OMPT2 chains C_{max}$	Tanaev et al. (1994)
* $OMPT2 r_i C_{max}$	Lawler et al. (1981,1982)
* $OMPT tree; p_{ij} = 1 L_{max}$	Timkovsky (2003)
* $OMPT2 L_{max}$	Lawler et al. (1981,1982)
* $OMPT2 \sum C_i$	Achugbue & Chin (1982)
* $OMPT2 chains; p_{ij} = 1 \sum w_i C_i$	Timkovsky (2003)
* $OMPT r_i; p_{ij} = 1 \sum U_i$	Kravchenko (1999)
* $OMPT2 chains; p_{ij} = 1 \sum U_i$	Timkovsky (2003)
* $OMPT2 chains; p_{ij} = 1 \sum T_i$	Timkovsky (2003)

• **minimal open:**

$FMPT chains; n = 2 C_{max}$	$JMPT2 chains; n = 2 \sum C_i$
$FMPT p_{ij} = 1 C_{max}$	$JMPT2 n = 3 \sum C_i$
$FMPT r_i; n = 2 C_{max}$	$JMPT2 p_{ij} = 1 \sum C_i$
$FMPT2 chains; p_{ij} = 1 C_{max}$	$JMPT2 r_i; n = 2 \sum C_i$
$FMPT2 r_i; p_{ij} = 1 L_{max}$	$OMPT n = 2 C_{max}$
$FMPT chains; n = 2 \sum C_i$	$OMPT p_{ij} = 1; n = 3 C_{max}$
$FMPT n = 3 \sum C_i$	$OMPT2 chains; p_{ij} = 1 C_{max}$
$FMPT p_{ij} = 1 \sum C_i$	$OMPT2 r_i; p_{ij} = 1 L_{max}$
$FMPT r_i; n = 2 \sum C_i$	$OMPT n = 2 \sum C_i$
$FMPT2 chains; p_{ij} = 1 \sum C_i$	$OMPT p_{ij} = 1; n = 3 \sum C_i$
$FMPT2 r_i; p_{ij} = 1 \sum w_i C_i$	$OMPT2 chains; p_{ij} = 1 \sum C_i$
$FMPT2 p_{ij} = 1 \sum w_i T_i$	$OMPT2 r_i; p_{ij} = 1 \sum w_i C_i$
$JMPT2 chains; n = 2 C_{max}$	$OMPT2 p_{ij} = 1 \sum w_i T_i$
$JMPT2 r_i; n = 2 C_{max}$	
$JMPT2 n = 3 L_{max}$	

• **maximal open:**

$FMPT tree; p_{ij} = 1 C_{max}$	$OMPT tree; p_{ij} = 1 C_{max}$
$FMPT chains; r_i; p_{ij} = 1 L_{max}$	$OMPT chains; r_i; p_{ij} = 1 L_{max}$
$FMPTm prec; r_i; p_{ij} = 1 L_{max}$	$OMPTm prec; r_i; p_{ij} = 1 L_{max}$
$FMPT prec; r_i; p_{ij} = 1 \sum C_i$	$OMPT prec; r_i; p_{ij} = 1 \sum C_i$
$FMPT prec; r_i; n = k \sum w_i C_i$	$OMPT prec; r_i; n = k \sum w_i C_i$
$FMPT r_i; p_{ij} = 1 \sum w_i U_i$	$OMPT p_{ij} = 1 \sum w_i U_i$
$FMPT r_i; p_{ij} = 1 \sum w_i T_i$	$OMPT prec; r_i; n = 2 \sum w_i U_i$
$JMPT2 p_{ij} = 1 \sum C_i$	$OMPT prec; r_i; p_{ij} = 1; n = k \sum w_i U_i$
$JMPT prec; r_i; n = 2 \sum w_i U_i$	$OMPTm r_i; p_{ij} = 1 \sum w_i U_i$
$JMPT2 prec; r_i; n = k \sum w_i U_i$	$OMPT prec; r_i; n = 2 \sum w_i T_i$
$JMPT prec; r_i; n = 2 \sum w_i T_i$	$OMPT prec; r_i; p_{ij} = 1; n = k \sum w_i T_i$
$JMPT2 prec; r_i; n = k \sum w_i T_i$	$OMPT r_i; p_{ij} = 1 \sum w_i T_i$

Multipurpose machine problems

- **maximal polynomially solvable:**

$QMPPM \sum C_i$	Horn (1973), Bruno et al. (1974)
$PMPM p_i = 1; r_i \sum w_i U_i$	Brucker et al. (1997)
$QMPPM p_i = 1 \sum w_i U_i$	Brucker et al. (1997)
$PMPM p_i = 1; r_i \sum w_i T_i$	Brucker et al. (1997)
$QMPPM p_i = 1 \sum w_i T_i$	Brucker et al. (1997)

- **minimal NP-hard:**

$PMPM2 C_{max}$	Lenstra et al. (1977)
$PMPM2 chains; p_i = 1 C_{max}$	Brucker et al. (1997)
* $PMPM C_{max}$	Garey & Johnson (1978)
* $PMPM intree; p_i = 1; r_i C_{max}$	Brucker et al. (1977)
* $PMPM prec; p_i = 1 C_{max}$	Ullman (1975)
* $PMPM2 chains C_{max}$	Du et al. (1991)
* $QMPPM chains; p_i = 1 C_{max}$	Kubiak (1988)
* $PMPM outtree; p_i = 1 L_{max}$	Brucker et al. (1977)
* $PMPM prec; p_i = 1 \sum C_i$	Lenstra & Rinnooy Kan (1978)
* $PMPM2 chains \sum C_i$	Du et al. (1991)
* $PMPM2 r_i \sum C_i$	Single-machine problem
$PMPM2 \sum w_i C_i$	Bruno et al. (1974)
* $PMPM \sum w_i C_i$	Lenstra (-)
* $PMPM2 chains; p_i = 1 \sum w_i C_i$	Timkovsky (1998)
* $PMPM2 chains; p_i = 1 \sum U_i$	Single-machine problem
* $PMPM2 chains; p_i = 1 \sum T_i$	Single-machine problem

- **minimal open:**

$QMPPM2 p_i = 1; r_i C_{max}$	$QMPPM2 p_i = 1; r_i \sum C_i$
$PMPM2 chains; p_i = 1 \sum C_i$	

- **maximal open:**

$QMPPM tree; p_i = 1; r_i \sum C_i$	$QMPPM p_i = 1; r_i \sum w_i U_i$
$QMPPM prec; p_i = 1; r_i \sum C_i$	$QMPPM p_i = 1; r_i \sum w_i T_i$

Shop problems with multipurpose machines

- **maximal polynomially solvable:**

$FMPMm r_i; p_{ij} = 1 C_{max}$	Brucker et al. (1997)
$FMPMm r_i; p_{ij} = 1 \sum C_i$	Brucker et al. (1997)
$FMPMm p_{ij} = 1 \sum w_i C_i$	Brucker et al. (1997)
$FMPMm p_{ij} = 1 \sum w_i U_i$	Brucker et al. (1997)
$FMPMm prec; r_i; n = k \sum w_i U_i$	Brucker (1995)
$FMPMm p_{ij} = 1 \sum T_i$	Brucker et al. (1997)
$FMPMm prec; r_i; n = k \sum w_i T_i$	Brucker (1995)
$JMPM prec; r_i; n = 2 L_{max}$	Jurisch (1995)
$JMPM prec; r_i; p_{ij} = 1; n = k \sum w_i U_i$	Brucker et al. (1997)
$JMPM prec; r_i; p_{ij} = 1; n = k \sum w_i T_i$	Brucker et al. (1997)
$OMPMm r_i; p_{ij} = 1 C_{max}$	Brucker et al. (1997)
$OMPMm r_i; p_{ij} = 1 \sum C_i$	Brucker et al. (1997)
$OMPMm p_{ij} = 1 \sum w_i C_i$	Brucker et al. (1997)
$OMPMm p_{ij} = 1 \sum w_i U_i$	Brucker et al. (1997)
$OMPMm prec; r_i; n = k \sum w_i U_i$	Brucker (1995)
$OMPMm p_{ij} = 1 \sum T_i$	Brucker et al. (1997)
$OMPMm prec; r_i; n = k \sum w_i T_i$	Brucker (1995)

- **maximal pseudopolynomially solvable:**

$JMPM2 n = 3 C_{max}$	Jurisch (1995), Meyer (1992)
$OMPM p_{ij} = 1 C_{max}$	Jurisch (1995)

- **minimal NP-hard:**

$FMPM n = 3 C_{max}$	Brucker et al. (1997)
$FMPM2 C_{max}$	Lenstra et al. (1977)
* $FMPM intree; r_i; p_{ij} = 1 C_{max}$	Brucker et al. (1977)
* $FMPM prec; p_{ij} = 1 C_{max}$	Ullman (1975)
* $FMPM2 chains C_{max}$	Lenstra et al. (1977)
* $FMPM2 r_i C_{max}$	Lenstra et al. (1977)
* $FMPM3 C_{max}$	Garey et al. (1976)
* $FMPM outtree; p_{ij} = 1 L_{max}$	Brucker et al. (1977)
* $FMPM2 L_{max}$	Lenstra et al. (1977)
* $FMPM prec; p_{ij} = 1 \sum C_i$	Lenstra & Rinnooy Kan (1978)
* $FMPM2 \sum C_i$	Garey et al. (1976)
* $FMPM2 chains; p_{ij} = 1 \sum w_i C_i$	Tanaev et al. (1994)
* $FMPM2 chains; p_{ij} = 1 \sum U_i$	Single-machine problem
* $FMPM2 chains; p_{ij} = 1 \sum T_i$	Single-machine problem
$JMPM2 n = 3 C_{max}$	Jurisch (1995), Meyer (1992)
* $JMPM2 chains; p_{ij} = 1 C_{max}$	Timkovsky (1985)
* $JMPM3 p_{ij} = 1 C_{max}$	Lenstra & Rinnooy Kan (1979)
$JMPM2 r_i; p_{ij} = 1 \sum C_i$	Timkovsky (1998)
$JMPM3 n = 3 \sum C_i$	Sotskov & Shakhlevich (1995)
* $JMPM2 chains; p_{ij} = 1 \sum C_i$	Timkovsky (1998)
* $JMPM3 p_{ij} = 1 \sum C_i$	Lenstra (-)
$JMPM2 p_{ij} = 1 \sum w_i C_i$	Timkovsky (1998)
* $JMPM2 r_i; p_{ij} = 1 \sum w_i C_i$	Timkovsky (1998)
$JMPM2 r_i; p_{ij} = 1 \sum U_i$	Timkovsky (1998)
$JMPM2 p_{ij} = 1 \sum w_i U_i$	Kravchenko (1999A)
* $JMPM2 p_{ij} = 1 \sum w_i T_i$	Timkovsky (1998)

$OMPM n = 3 C_{max}$	Gonzalez & Sahni (1976)
$OMPM3 C_{max}$	Gonzalez & Sahni (1976)
* $OMPM C_{max}$	Lenstra (-)
* $OMPM outtree; r_i; p_{ij} = 1 C_{max}$	Timkovsky (2003)
* $OMPM prec; p_{ij} = 1 C_{max}$	Timkovsky (2003)
* $OMPM2 chains C_{max}$	Tanaev et al. (1994)
* $OMPM2 r_i C_{max}$	Lawler et al. (1981,1982)
* $OMPM outtree; p_{ij} = 1 L_{max}$	Timkovsky (2003)
* $OMPM2 L_{max}$	Lawler et al. (1981,1982)
* $OMPM2 \sum C_i$	Achugbue & Chin (1982)
* $OMPM prec; p_{ij} = 1 \sum C_i$	Lenstra & Rinnooy Kan (1978)
* $OMPM2 chains; p_{ij} = 1 \sum w_i C_i$	Timkovsky (2003)
* $OMPM r_i; p_{ij} = 1 \sum U_i$	Kravchenko (1999)
* $OMPM2 chains; p_{ij} = 1 \sum U_i$	Timkovsky (2003)
* $OMPM2 chains; p_{ij} = 1 \sum T_i$	Timkovsky (2003)

• **minimal open:**

$FMPM p_{ij} = 1 C_{max}$	$JMPM2 p_{ij} = 1 C_{max}$	$OMPM2 chains; p_{ij} = 1 C_{max}$
$FMPM2 chains; p_{ij} = 1 C_{max}$	$JMPM2 n = 2 \sum C_i$	$OMPM2 r_i; p_{ij} = 1 L_{max}$
$FMPM2 r_i; p_{ij} = 1 L_{max}$	$JMPM2 p_{ij} = 1 \sum C_i$	$OMPM p_{ij} = 1; n = 2 \sum C_i$
$FMPM n = 2 \sum C_i$	$JMPM2 n = 2 \sum U_i$	$OMPM p_{ij} = 1; n = 3 \sum C_i$
$FMPM p_{ij} = 1 \sum C_i$	$OMPM p_{ij} = 1; n = 2 C_{max}$	$OMPM2 chains; p_{ij} = 1 \sum C_i$
$FMPM2 chains; p_{ij} = 1 \sum C_i$	$OMPM p_{ij} = 1; n = 3 C_{max}$	$OMPM2 r_i; p_{ij} = 1 \sum w_i C_i$
$FMPM2 r_i; p_{ij} = 1 \sum w_i C_i$	$OMPM2 C_{max}$	$OMPM2 p_{ij} = 1 \sum w_i T_i$
$FMPM n = 2 \sum U_i$		
$FMPM2 p_{ij} = 1 \sum w_i T_i$		

• **maximal open:**

$FMPM outtree; r_i; p_{ij} = 1 C_{max}$	$OMPM tree; p_{ij} = 1 C_{max}$
$FMPM tree; p_{ij} = 1 C_{max}$	$OMPM2 C_{max}$
$FMPM chains; r_i; p_{ij} = 1 L_{max}$	$OMPM intree; r_i; p_{ij} = 1 L_{max}$
$FMPM intree; p_{ij} = 1 L_{max}$	$OMPMm prec; r_i; p_{ij} = 1 L_{max}$
$FMPMm prec; r_i; p_{ij} = 1 L_{max}$	$OMPM tree; r_i; p_{ij} = 1 \sum C_i$
$FMPM tree; r_i; p_{ij} = 1 \sum C_i$	$OMPMm prec; r_i; p_{ij} = 1 \sum C_i$
$FMPMm prec; r_i; p_{ij} = 1 \sum C_i$	$OMPM prec; r_i; n = k \sum w_i C_i$
$FMPM prec; r_i; n = k \sum w_i C_i$	$OMPM p_{ij} = 1 \sum w_i U_i$
$FMPM r_i; p_{ij} = 1 \sum w_i U_i$	$OMPM prec; r_i; n = 2 \sum w_i U_i$
$FMPM r_i; p_{ij} = 1 \sum w_i T_i$	$OMPM prec; r_i; p_{ij} = 1; n = k \sum w_i U_i$
$JMPM2 r_i; p_{ij} = 1 L_{max}$	$OMPMm r_i; p_{ij} = 1 \sum w_i U_i$
$JMPM2 prec; r_i; n = k \sum w_i C_i$	$OMPM prec; r_i; n = 2 \sum w_i T_i$
$JMPM2 p_{ij} = 1 \sum U_i$	$OMPM prec; r_i; p_{ij} = 1; n = k \sum w_i T_i$
$JMPM prec; r_i; n = 2 \sum w_i U_i$	$OMPM r_i; p_{ij} = 1 \sum w_i T_i$
$JMPM2 p_{ij} = 1 \sum T_i$	
$JMPM prec; r_i; n = 2 \sum w_i T_i$	

Serial batching problems

- **maximal polynomially solvable:**

$1 prec; s - batch L_{max}$	Ng et al. (2002)
$1 prec; p_i = p; s - batch \sum C_i$	Albers & Brucker (1993)
$1 s - batch \sum C_i$	Coffman et al. (1990)
$1 p_i = p; s - batch; r_i \sum w_i C_i$	Baptiste (2000A)
$1 s - batch \sum U_i$	Brucker & Kovalyov (1996)
$1 p_i = p; s - batch; r_i \sum w_i U_i$	Baptiste (2000A)
$1 p_i = p; s - batch; r_i \sum T_i$	Baptiste (2000A)

- **maximal pseudopolynomially solvable:**

$1 s - batch \sum w_i U_i$	Brucker & Kovalyov (1996), Karp (1972)
$1 s - batch \sum T_i$	Du & Leung (1990), Baptiste & Jouglet (2001)

- **minimal NP-hard:**

* $1 s - batch; r_i L_{max}$	Lenstra et al. (1977)
$1 chains; s - batch \sum C_i$	Albers & Brucker (1993)
* $1 prec; s - batch \sum C_i$	Lawler (1978), Lenstra & Rinnooy Kan (1978)
* $1 s - batch; r_i \sum C_i$	Lenstra et al. (1977)
* $1 chains; p_i = 1; s - batch \sum w_i C_i$	Albers & Brucker (1993)
* $1 s - batch \sum w_i C_i$	Albers & Brucker (1993)
* $1 chains; p_i = 1; s - batch \sum U_i$	Lenstra & Rinnooy Kan (1980)
$1 s - batch \sum w_i U_i$	Brucker & Kovalyov (1996), Karp (1972)
$1 s - batch \sum T_i$	Du & Leung (1990), Baptiste & Jouglet (2001)
* $1 chains; p_i = 1; s - batch \sum T_i$	Leung & Young (1990)

- **minimal open:**

$1 chains; p_i = 1; s - batch; r_i L_{max}$
$1 chains; p_i = 1; s - batch; r_i \sum C_i$
$1 p_i = 1; s - batch \sum w_i T_i$

- **maximal open:**

$1 prec; p_i = p; s - batch; r_i L_{max}$
$1 prec; p_i = p; s - batch; r_i \sum C_i$
$1 p_i = p; s - batch; r_i \sum w_i T_i$

Parallel batching problems

- **maximal polynomially solvable:**

$1 outtree;p_i = p;p - batch;r_i;b < n C_{max}$	Parallel machine problem
$1 p - batch;b < n C_{max}$	Brucker et al. (1998)
$1 tree;p_i = p;p - batch;b < n C_{max}$	Parallel machine problem
$1 chains;p_i = 1;p - batch;r_i;b < n L_{max}$	Parallel machine problem
$1 intree;p_i = p;p - batch;b < n L_{max}$	Parallel machine problem
$1 outtree;p_i = 1;p - batch;r_i;b < n \sum C_i$	Parallel machine problem
$1 tree;p_i = p;p - batch;b < n \sum C_i$	Parallel machine problem
$1 p - batch \sum w_i C_i$	Brucker et al. (1998)
$1 p_i = p;p - batch;r_i;b < n \sum w_i C_i$	Baptiste (2000A)
$1 p - batch \sum U_i$	Brucker et al. (1998)
$1 p_i = p;p - batch;r_i;b < n \sum w_i U_i$	Baptiste (2000A)
$1 prec;p_i = p;p - batch \sum w_i U_i$	Earliest Start Schedule
$1 p_i = p;p - batch;r_i;b < n \sum T_i$	Baptiste (2000A)
$1 p_i = 1;p - batch;r_i;b < n \sum w_i T_i$	Parallel machine problem
$1 p_i = p;p - batch;b < n \sum w_i T_i$	Parallel machine problem
$1 p_i = p;p - batch;r_i \sum w_i T_i$	Baptiste et al. (2004)
$1 prec;p_i = p;p - batch \sum w_i T_i$	Earliest Start Schedule

- **maximal pseudopolynomially solvable:**

$1 p - batch;r_i \sum w_i U_i$	Baptiste et al. (2004)
$1 p - batch;r_i \sum w_i T_i$	Baptiste et al. (2004)

- **minimal NP-hard:**

* $1 intree;p_i = 1;p - batch;r_i;b < n C_{max}$	Parallel machine problem
* $1 p - batch;r_i;b < n C_{max}$	Brucker et al. (1998)
* $1 prec;p_i = 1;p - batch;b < n C_{max}$	Parallel machine problem
* $1 outtree;p_i = 1;p - batch;b < n L_{max}$	Parallel machine problem
* $1 p - batch;b < n L_{max}$	Brucker et al. (1998)
* $1 intree;p_i = 1;p - batch;r_i;b < n \sum C_i$	Parallel machine problem
* $1 p - batch;r_i;b < n \sum C_i$	Single machine problem
* $1 prec;p_i = 1;p - batch;b < n \sum C_i$	Parallel machine problem
* $1 chains;p_i = 1;p - batch;b < n \sum w_i C_i$	Parallel machine problem
* $1 chains;p_i = 1;p - batch;b < n \sum U_i$	Single machine problem
$1 p - batch \sum w_i U_i$	Brucker et al. (1998)
* $1 chains;p_i = 1;p - batch;b < n \sum T_i$	Single machine problem
$1 p - batch \sum w_i T_i$	Brucker et al. (1998)

- **minimal open:**

$1 chains;p - batch C_{max}$	$1 p - batch;b < n \sum C_i$
$1 intree;p_i = 1;p - batch;r_i C_{max}$	$1 p - batch;r_i \sum C_i$
$1 p - batch;r_i C_{max}$	$1 chains;p_i = 1;p - batch;r_i \sum w_i C_i$
$1 chains;p_i = p;p - batch;r_i L_{max}$	$1 chains;p_i = 1;p - batch;r_i \sum U_i$
$1 outtree;p_i = 1;p - batch;r_i L_{max}$	$1 chains;p_i = 1;p - batch;r_i \sum T_i$
$1 chains;p - batch \sum C_i$	$1 p - batch \sum T_i$
$1 chains;p_i = p;p - batch;r_i \sum C_i$	$1 p_i = p;p - batch;r_i;b < n \sum w_i T_i$
$1 intree;p_i = 1;p - batch;r_i \sum C_i$	

- **maximal open:**

$1 tree;p - batch;b < n C_{max}$	$1 prec;p - batch;r_i \sum U_i$
$1 chains;p_i = p;p - batch;r_i;b < n L_{max}$	$1 prec;p_i = p;p - batch;r_i \sum w_i U_i$
$1 outtree;p_i = p;p - batch;r_i;b < n \sum C_i$	$1 prec;p - batch;r_i \sum T_i$
$1 tree;p - batch;b < n \sum C_i$	$1 p_i = p;p - batch;r_i;b < n \sum w_i T_i$
$1 p - batch;b < n \sum w_i C_i$	$1 prec;p_i = p;p - batch;r_i \sum w_i T_i$
$1 prec;p - batch;r_i \sum w_i C_i$	

Single machine problems with non-negative time-lags

- **maximal polynomially solvable:**

$1 chains(l); p_i = p C_{max}$	Munier & Sourd (2003)
$1 outtree(l); p_i = 1; r_i C_{max}$	Bruno et al. (1980)
$1 prec(1) C_{max}$	Finta & Liu (1996)
$1 prec; r_i C_{max}$	Lawler (1973)
$1 tree(l); p_i = 1 C_{max}$	Bruno et al. (1980)
$1 intree(l); p_i = 1 L_{max}$	Bruno et al. (1980)
$1 prec L_{max}$	Lawler (1973)
$1 prec(1); p_i = 1; r_i L_{max}$	Bruno et al. (1980)
$1 prec; p_i = p; r_i L_{max}$	Simons (1978)
$1 chains(l); p_i = p \sum C_i$	Brucker et al. (2006)
$1 outtree(l); p_i = 1; r_i \sum C_i$	Brucker & Knust (1999)
$1 prec(1); p_i = 1; r_i \sum C_i$	Baptiste & Timkovsky (2004)
$1 prec; p_i = p; r_i \sum C_i$	Simons (1983)
$1 p_i = p; r_i \sum w_i C_i$	Baptiste (2000)
$1 sp - graph \sum w_i C_i$	Lawler (1978)
$1 \sum U_i$	Moore (1968), Maxwell (1970), Sidney (1973)
$1 p_i = p; r_i \sum w_i U_i$	Baptiste (1999)
$1 p_i = p; r_i \sum T_i$	Baptiste (2000)
$1 p_i = 1; r_i \sum w_i T_i$	Assignment-problem
$1 p_i = p \sum w_i T_i$	Assignment-problem

- **maximal pseudopolynomially solvable:**

$1 \sum w_i U_i$	Lawler & Moore (1969), Karp (1972)
$1 \sum T_i$	Lawler (1977), Du & Leung (1990)

- **minimal NP-hard:**

* $1 chains(l) C_{max}$	Wikum et al. (1994)
* $1 chains(l_{ij}); p_i = 1 C_{max}$	Yu (1996), Yu et al. (2004)
* $1 intree(l); p_i = 1; r_i C_{max}$	Brucker & Knust (1999)
* $1 prec(l); p_i = 1 C_{max}$	Leung et al. (1984), Timkovsky (2003)
* $1 outtree(l); p_i = 1 L_{max}$	Brucker & Knust (1999)
* $1 r_i L_{max}$	Lenstra et al. (1977)
* $1 chains(l) \sum C_i$	Brucker & Knust (1999)
* $1 prec \sum C_i$	Lawler (1978), Lenstra & Rinnooy Kan (1978)
* $1 r_i \sum C_i$	Lenstra et al. (1977)
* $1 chains(1); p_i = 1 \sum w_i C_i$	Tanaev et al. (1994)
* $1 chains; p_i = 1; r_i \sum w_i C_i$	Lenstra & Rinnooy Kan (1980)
* $1 prec; p_i = 1 \sum w_i C_i$	Lawler (1978), Lenstra & Rinnooy Kan (1978)
* $1 chains; p_i = 1 \sum U_i$	Lenstra & Rinnooy Kan (1980)
$1 \sum w_i U_i$	Lawler & Moore (1969), Karp (1972)
$1 \sum T_i$	Lawler (1977), Du & Leung (1990)
* $1 chains; p_i = 1 \sum T_i$	Leung & Young (1990)
* $1 \sum w_i T_i$	Lawler (1977), Lenstra et al. (1977)

- **minimal open:**

$1 chains(1); p_i = p; r_i C_{max}$	$1 chains(l_{ij}); p_i = 1 \sum C_i$
$1 intree(l); p_i = p C_{max}$	$1 intree(1); p_i = 1; r_i \sum C_i$
$1 outtree(l); p_i = p C_{max}$	$1 intree(1); p_i = p \sum C_i$
$1 chains(1); p_i = p L_{max}$	$1 intree(l); p_i = 1 \sum C_i$
$1 chains(l); p_i = 1; r_i L_{max}$	$1 outtree(1); p_i = p \sum C_i$
$1 chains(1) \sum C_i$	$1 p_i = p; r_i \sum w_i T_i$
$1 chains(1); p_i = p; r_i \sum C_i$	

- **maximal open:**

$1 outtree(l); p_i = p; r_i C_{max}$	$1 prec(1) L_{max}$
$1 prec(1); r_i C_{max}$	$1 prec(1); p_i = p; r_i L_{max}$
$1 tree(l); p_i = p C_{max}$	$1 prec(l_{ij}); p_i = p; r_i \sum C_i$
$1 chains(l); p_i = p; r_i L_{max}$	$1 tree(1) \sum C_i$
$1 intree(l); p_i = p L_{max}$	$1 p_i = p; r_i \sum w_i T_i$

Flow-shop problems with transportation delays

- **maximal polynomially solvable:**

$F2 p_{ij} = 1; t_i \in \{T_1, T_2\} C_{max}$	Yu (1996)
$F2 t_{ik} = T C_{max}$	Johnson (1954)
$F p_{ij} = 1; t_i \sum C_i$	Brucker et al. (2004)
$F p_{ij} = 1; t_k; r_i \sum w_i U_i$	Single-machine problem
$F p_{ij} = 1; t_k; r_i \sum w_i T_i$	Single-machine problem

- **minimal NP-hard:**

* $F2 p_{ij} = 1; t_i C_{max}$	Yu (1996), Yu et al. (2004)
* $F2 r_i C_{max}$	Lenstra et al. (1977)
* $F2 t_i \in \{T_1, T_2\} C_{max}$	Yu (1996)
* $F3 C_{max}$	Garey et al. (1976)
* $F2 L_{max}$	Lenstra et al. (1977)
* $F2 \sum C_i$	Garey et al. (1976)
* $F2 p_{ij} = 1; t_i; r_i \sum C_i$	Brucker et al. (2004)
* $F2 p_{ij} = 1; t_i \sum w_i C_i$	Brucker et al. (2004)

- **minimal open:**

$F2 p_{ij} = 1; t_i \in \{T_1, T_2\}; r_i C_{max}$	$F2 p_{ij} = 1; t_i \in \{T_1, T_2\}; r_i \sum C_i$	$F2 p_{ij} = 1; t_i \in \{T_1, T_2\} \sum w_i C_i$
$F3 p_{ij} = 1; t_i \in \{T_1, T_2\} C_{max}$	$F3 p_{ij} = 1; t_i \in \{T_1, T_2\}; r_i \sum C_i$	$F3 p_{ij} = 1; t_i \in \{T_1, T_2\} \sum w_i C_i$
$F2 p_{ij} = 1; t_i \in \{T_1, T_2\} L_{max}$	$F3 p_{ij} = 1; t_{ik} \sum C_i$	

- **maximal open:**

$F p_{ij} = 1; t_{ik} \sum C_i$	$F p_{ij} = 1; t_i \in \{T_1, T_2\}; r_i \sum w_i U_i, \sum w_i T_i$	$F3 p_{ij} = 1; t_{ik}; r_i \sum w_i U_i, \sum w_i T_i$
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Open-shop problems with transportation delays

- **maximal polynomially solvable:**

$O p_{ij} = 1; t_{ikl} = T C_{max}$	Rayward-Smith & Rebaine (1992)
$O2 C_{max}$	Gonzalez & Sahni (1976)
$O2 p_{ij} = 1; t_{ikl} = T; r_i C_{max}$	Brucker et al. (2004)
$O2 p_{ij} = 1; t_{kl} C_{max}$	Knust (1999), Brucker et al. (2004)
$O p_{ij} = 1; r_i L_{max}$	Brucker et al. (1993), Networkflowproblem
$Om p_{ij} = 1; r_i \sum C_i$	Tautenhahn & Woeginger (1997)
$O p_{ij} = 1 \sum w_i C_i$	Brucker et al. (1993)
$O2 p_{ij} = 1; t_{kl} \sum w_i C_i$	Brucker et al. (2004)
$O p_{ij} = 1 \sum U_i$	Liu & Bulfin (1988)
$O2 p_{ij} = 1; t_{ikl} = T \sum U_i$	Brucker et al. (2004)
$Om p_{ij} = 1; r_i \sum w_i U_i$	Baptiste (2003)
$O p_{ij} = 1 \sum T_i$	Liu & Bulfin (1988)

- **minimal NP-hard:**

$O2 t_{ikl} = T C_{max}$	Yu (1996)
$O3 C_{max}$	Gonzalez & Sahni (1976)
* $O C_{max}$	Lenstra (-)
* $O p_{ij} = 1; t_{kl} = t_{lk} C_{max}$	Rayward-Smith & Rebaine (1992)
* $O2 p_{ij} = 1; t_i C_{max}$	Yu (1996), Yu et al. (2004)
* $O2 r_i C_{max}$	Lawler et al. (1981,1982)
* $O2 t_i \in \{T_1, T_2\} C_{max}$	Yu (1996)
* $O2 L_{max}$	Lawler et al. (1981,1982)
* $O2 \sum C_i$	Achugbue & Chin (1982)
* $O2 p_{ij} = 1; t_i; r_i \sum C_i$	Brucker et al. (2004)
* $O2 p_{ij} = 1; t_i \sum w_i C_i$	Brucker et al. (2004)
* $O p_{ij} = 1; r_i \sum U_i$	Kravchenko (1999)

- **minimal open:**

$O2 p_{ij} = 1; t_i \in \{T_1, T_2\} C_{max}$	$O3 p_{ij} = 1; t_{ikl} = T L_{max}$	$O p_{ij} = 1 \sum w_i U_i$
$O2 p_{ij} = 1; t_{kl}; r_i C_{max}$	$O p_{ij} = 1; r_i \sum C_i$	$O2 p_{ij} = 1; t_{ikl} = T \sum w_i U_i$
$O3 p_{ij} = 1; t_i \in \{T_1, T_2\} C_{max}$	$O2 p_{ij} = 1; t_i \in \{T_1, T_2\} \sum C_i$	$O2 p_{ij} = 1; r_i \sum T_i$
$O3 p_{ij} = 1; t_{ikl} = T; r_i C_{max}$	$O2 p_{ij} = 1; t_{ikl} = T; r_i \sum C_i$	$O2 p_{ij} = 1; t_{ikl} = T \sum T_i$
$O3 p_{ij} = 1; t_{kl} = t_{lk} C_{max}$	$O3 p_{ij} = 1; t_{ikl} = T \sum C_i$	$O3 p_{ij} = 1; r_i \sum T_i$
$O2 p_{ij} = 1; t_{ikl} = T; r_i L_{max}$	$O2 p_{ij} = 1; r_i \sum w_i C_i$	$O2 p_{ij} = 1 \sum w_i T_i$
$O2 p_{ij} = 1; t_{kl} L_{max}$	$O3 p_{ij} = 1; r_i \sum w_i C_i$	$O3 p_{ij} = 1 \sum w_i T_i$

- **maximal open:**

$O p_{ij} = 1; t_{ikl} \sum C_i$	$Om p_{ij} = 1; t_{kl}; r_i \sum w_i U_i$
$O p_{ij} = 1; t_{kl}; r_i \sum w_i C_i$	$O p_{ij} = 1; t_i \in \{T_1, T_2\}; r_i \sum w_i T_i$
$O p_{ij} = 1; t_i \in \{T_1, T_2\} \sum w_i U_i$	$O3 p_{ij} = 1; t_{ikl}; r_i \sum w_i T_i$
$O3 p_{ij} = 1; t_{ikl}; r_i \sum w_i U_i$	$Om p_{ij} = 1; t_{kl}; r_i \sum w_i T_i$
$Om p_{ij} = 1; t_i \in \{T_1, T_2\}; r_i \sum w_i U_i$	

Flow-shop problems with transportation times and a single robot

- maximal polynomially solvable:

$F2 C_{max}$	Johnson (1954)
$F2; R1 p_{ij} = 1; t_i C_{max}$	Hurink & Knust (2001)
$F2; R1 p_{ij} = p; t_i \in \{T_1, T_2\} C_{max}$	Hurink & Knust (2001)
$F3; R1 p_{ij} = 1; t_k; r_i C_{max}$	Baptiste et al. (2004)
$F; R1 n \geq m - 1; p_{ij} = p; t_k C_{max}$	Hurink & Knust (2001)
$F3; R1 p_{ij} = 1; t_k L_{max}$	Baptiste et al. (2004)
$F p_{ij} = p; r_i \sum w_i C_i$	Single-machine problem
$F2; R1 p_{ij} = p; t_{ik} = T; r_i \sum w_i C_i$	Knust (1999)
$F p_{ij} = p; r_i \sum w_i U_i$	Single-machine problem
$F2; R1 p_{ij} = p; t_{ik} = T; r_i \sum w_i U_i$	Knust (1999)
$F p_{ij} = p; r_i \sum T_i$	Single-machine problem
$F2; R1 p_{ij} = p; t_{ik} = T; r_i \sum T_i$	Knust (1999)
$F p_{ij} = 1; r_i \sum w_i T_i$	Single-machine problem
$F p_{ij} = p \sum w_i T_i$	Single-machine problem
$F2; R1 p_{ij} = p; t_{ik} = T \sum w_i T_i$	Knust (1999)

- minimal NP-hard:

* $F2 r_i C_{max}$	Lenstra et al. (1977)
* $F2; R1 p_{ij} = p; t_i C_{max}$	Hurink & Knust (2001)
* $F2; R1 t_{ik} = T C_{max}$	Kise (1991), Hurink & Knust (2001)
* $F3 C_{max}$	Garey et al. (1976)
* $F3; R1 p_{ij} = p; t_{ik}; r_i C_{max}$	Knust (1999)
* $F2 L_{max}$	Lenstra et al. (1977)
* $F2; R1 p_{ij} = 1; t_i; r_i L_{max}$	Knust (1999)
* $F3; R1 p_{ij} = 1; t_{ik}; r_i L_{max}$	Knust (1999)
* $F3; R1 p_{ij} = p; t_{ik} L_{max}$	Knust (1999)
* $F2 \sum C_i$	Garey et al. (1976)
* $F2; R1 p_{ij} = 1; t_i; r_i \sum C_i$	Knust (1999)
* $F3; R1 p_{ij} = 1; t_{ik}; r_i \sum C_i$	Knust (1999)
$F2; R1 p_{ij} = 1; t_i \sum w_i U_i$	Knust (1999)
$F3; R1 p_{ij} = 1; t_{ik} \sum w_i U_i$	Knust (1999)
$F2; R1 p_{ij} = 1; t_i \sum T_i$	Knust (1999)
$F3; R1 p_{ij} = 1; t_{ik} \sum T_i$	Knust (1999)
* $F2; R1 p_{ij} = 1; t_i \sum w_i T_i$	Knust (1999)
* $F3; R1 p_{ij} = 1; t_{ik} \sum w_i T_i$	Knust (1999)

- minimal open:

$F2; R1 p_{ij} = 1; t_i \in \{T_1, T_2\}; r_i C_{max}$	$Fm; R1 p_{ij} = 1; t_{ik} = T L_{max}$
$F3; R1 p_{ij} = 1; t_i \in \{T_1, T_2\} C_{max}$	$F2; R1 p_{ij} = 1; t_i \in \{T_1, T_2\} \sum C_i$
$F3; R1 p_{ij} = p; t_{ik} = T; r_i C_{max}$	$F3; R1 p_{ij} = 1; t_{ik} = T \sum C_i$
$Fm; R1 p_{ij} = 1; t_{ik} = T; r_i C_{max}$	$F3; R1 p_{ij} = 1; t_{ik} = T \sum U_i$
$F2; R1 p_{ij} = 1; t_i \in \{T_1, T_2\} L_{max}$	$F2 p_{ij} = p; r_i \sum w_i T_i$
$F3; R1 p_{ij} = 1; t_{ik} = T; r_i L_{max}$	$F2; R1 p_{ij} = 1; t_{ik} = T; r_i \sum w_i T_i$
$F3; R1 p_{ij} = p; t_{ik} = T L_{max}$	$F3 p_{ij} = p; r_i \sum w_i T_i$

- maximal open:

$F3; R1 p_{ij} = p; t_{ik} C_{max}$	$F; R1 p_{ij} = p; t_i \in \{T_1, T_2\}; r_i \sum w_i U_i$
$F; R1 p_{ij} = 1; t_{ik}; r_i C_{max}$	$F; R1 p_{ij} = p; t_k; r_i \sum w_i U_i$
$F; R1 p_{ij} = p; t_{ik} \sum w_i C_i$	$F3; R1 p_{ij} = p; t_i; r_i \sum w_i T_i$
$F; R1 p_{ij} = 1; t_{ik} \sum U_i$	$F; R1 p_{ij} = p; t_i \in \{T_1, T_2\}; r_i \sum w_i T_i$
$F3; R1 p_{ij} = p; t_i; r_i \sum w_i U_i$	$F; R1 p_{ij} = p; t_k; r_i \sum w_i T_i$

Parallel machine problems with a single server

- **maximal polynomially solvable:**

$P; S1 s_i = s; p_i = p; r_i C_{max}$	Brucker et al. (2002B)
$P \sum C_i$	Bruno et al. (1974)
$P2; S1 s_i = 1 \sum C_i$	Hall et al. (2000)
$P; S1 s_i = s; p_i = p; r_i \sum C_i$	Brucker et al. (2002B)
$P; S1 p_i = 1 \sum w_i C_i$	Hall et al. (2000)
$P; S1 s_i = s; p_i = 1; r_i \sum w_i C_i$	Brucker et al. (2002B)
$P p_i = p; r_i \sum w_i C_i$	Brucker & Kravchenko (2008)
$P; S1 p_i = 1 \sum U_i$	Hall et al. (2000)
$P; S1 s_i = s; p_i = 1; r_i \sum w_i U_i$	Brucker et al. (2002B)
$Pm p_i = p; r_i \sum w_i U_i$	Baptiste et al. (2004)
$P; S1 s_i = s; p_i = p \sum w_i U_i$	Assignment problem
$P; S1 s_i = s; p_i = 1; r_i \sum T_i$	Brucker et al. (2002B)
$P p_i = p; r_i \sum T_i$	Brucker & Kravchenko (2005)
$P p_i = 1; r_i \sum w_i T_i$	Networkflowproblem
$P; S1 s_i = 1; p_i = 1; r_i \sum w_i T_i$	Assignment problem
$P; S1 s_i = s; p_i = p \sum w_i T_i$	Assignment problem

- **maximal pseudopolynomially solvable:**

$P2; S1 s_i = 1 C_{max}$	Hall et al. (2000), Kravchenko & Werner (1997)
$Pm r_i C_{max}$	Lawler et al. (1989)
$Pm \sum w_i C_i$	Lawler et al. (1989)
$P2; S1 p_i = 1 \sum w_i U_i$	Single-machine problem, Hall et al. (2000)
$Pm \sum w_i U_i$	Lawler et al. (1989)
$P2; S1 p_i = 1 \sum T_i$	Single-machine problem, Hall et al. (2000)

- **minimal NP-hard:**

$P2 C_{max}$	Lenstra et al. (1977)
$P2; S1 p_i = p C_{max}$	Brucker et al. (2002B)
* $P C_{max}$	Garey & Johnson (1978)
* $P2; S1 s_i = s C_{max}$	Hall et al. (2000)
* $P2; S1 p_i = 1; r_i L_{max}$	Single-machine problem, Brucker et al. (2002B)
* $P2; S1 s_i = 1 L_{max}$	Hall et al. (2000)
$P2; S1 p_i = p \sum C_i$	Brucker et al. (2002B)
* $P2 r_i \sum C_i$	Single-machine problem
* $P2; S1 p_i = 1; r_i \sum C_i$	Single-machine problem, Brucker et al. (2002B)
* $P2; S1 s_i = s \sum C_i$	Hall et al. (2000)
* $P; S1 s_i = 1 \sum C_i$	Brucker et al. (2002B)
$P2 \sum w_i C_i$	Bruno et al. (1974)
* $P \sum w_i C_i$	Lenstra (-)
$P2; S1 p_i = 1 \sum w_i U_i$	Single-machine problem, Hall et al. (2000)
$P2; S1 p_i = 1 \sum T_i$	Single-machine problem, Hall et al. (2000)
* $P2; S1 p_i = 1 \sum w_i T_i$	Single-machine problem, Hall et al. (2000)

- **minimal open:**

$P2; S1 p_i = 1; r_i C_{max}$	$P p_i = p; r_i \sum U_i$
$P2; S1 s_i = 1; p_i = p; r_i L_{max}$	$P2 p_i = p; r_i \sum w_i T_i$
$Pm; S1 s_i = 1 \sum C_i$	$P2; S1 s_i = s; p_i = 1; r_i \sum w_i T_i$
$P2; S1 s_i = 1; p_i = p; r_i \sum w_i C_i$	

- **maximal open:**

$P; S1 p_i = 1; r_i C_{max}$	$P; S1 s_i = s; p_i = p; r_i \sum w_i U_i$
$Pm; S1 s_i = 1 \sum C_i$	$P; S1 s_i = s; p_i = p; r_i \sum w_i T_i$

Flow-shop problems with a single server

- maximal polynomially solvable:

$F2 C_{max}$	Johnson (1954)
$F2; S1 p_{ij} = p; s_{ij} = s; r_i C_{max}$	Brucker et al. (2005)
$F; S1 p_{ij} = 1; s_{ij} = s; r_i C_{max}$	Brucker et al. (2005)
$F; S1 p_{ij} = p; s_{ij} = s C_{max}$	Brucker et al. (2005)
$F2; S1 p_{ij} = p; s_{ij} = s; r_i \sum C_i$	Brucker et al. (2005)
$F; S1 p_{ij} = 1; s_{ij} = s; r_i \sum C_i$	Brucker et al. (2005)
$F p_{ij} = p; r_i \sum w_i C_i$	Single-machine problem
$F2; S1 p_{ij} = p; s_{ij} = 1; r_i \sum w_i C_i$	Single-machine problem
$F p_{ij} = p; r_i \sum w_i U_i$	Single-machine problem
$F2; S1 p_{ij} = p; s_{ij} = 1; r_i \sum w_i U_i$	Single-machine problem
$F2; S1 p_{ij} = p; s_{ij} = s \sum w_i U_i$	Assignment problem
$F; S1 p_{ij} = 1; s_{ij} = s \sum w_i U_i$	Assignment problem
$F p_{ij} = p; r_i \sum T_i$	Single-machine problem
$F2; S1 p_{ij} = p; s_{ij} = 1; r_i \sum T_i$	Single-machine problem
$F p_{ij} = 1; r_i \sum w_i T_i$	Single-machine problem
$F p_{ij} = p \sum w_i T_i$	Single-machine problem
$F2; S1 p_{ij} = p; s_{ij} = s \sum w_i T_i$	Assignment problem
$F; S1 p_{ij} = 1; s_{ij} = s \sum w_i T_i$	Assignment problem

- minimal NP-hard:

$F2; S1 p_{ij} = p C_{max}$	Brucker et al. (2005)
* $F2 r_i C_{max}$	Lenstra et al. (1977)
* $F2; S1 s_{ij} = s C_{max}$	Brucker et al. (2005)
* $F3 C_{max}$	Garey et al. (1976)
* $F2 L_{max}$	Lenstra et al. (1977)
* $F2; S1 p_{ij} = 1; r_i L_{max}$	Brucker et al. (2005)
* $F3; S1 p_{ij} = 1; r_i L_{max}$	Brucker et al. (2005)
* $F2 \sum C_i$	Garey et al. (1976)
* $F2; S1 p_{ij} = 1; r_i \sum C_i$	Brucker et al. (2005)
* $F3; S1 p_{ij} = 1; r_i \sum C_i$	Brucker et al. (2005)
$F2; S1 p_{ij} = 1 \sum w_i U_i$	Brucker et al. (2005)
$F3; S1 p_{ij} = 1 \sum w_i U_i$	Brucker et al. (2005)
$F2; S1 p_{ij} = 1 \sum T_i$	Brucker et al. (2005)
$F3; S1 p_{ij} = 1 \sum T_i$	Brucker et al. (2005)
* $F2; S1 p_{ij} = 1 \sum w_i T_i$	Brucker et al. (2005)
* $F3; S1 p_{ij} = 1 \sum w_i T_i$	Brucker et al. (2005)

- minimal open:

$F2; S1 p_{ij} = 1 C_{max}$	$F3; S1 p_{ij} = 1; s_{ij} = 1; r_i L_{max}$	$F2; S1 p_{ij} = 1; s_{ij} = s; r_i \sum w_i C_i$
$F2; S1 s_{ij} = 1 C_{max}$	$F3; S1 p_{ij} = p; s_{ij} = 1 L_{max}$	$F3; S1 p_{ij} = 1; s_{ij} = 1; r_i \sum w_i C_i$
$F3; S1 p_{ij} = 1 C_{max}$	$F2; S1 p_{ij} = 1 \sum C_i$	$F2 p_{ij} = p; r_i \sum w_i T_i$
$F3; S1 p_{ij} = p; s_{ij} = 1; r_i C_{max}$	$F3; S1 p_{ij} = 1 \sum C_i$	$F2; S1 p_{ij} = 1; s_{ij} = 1; r_i \sum w_i T_i$
$F2; S1 p_{ij} = 1; s_{ij} = s; r_i L_{max}$	$F3; S1 p_{ij} = p; s_{ij} = 1 \sum C_i$	$F3 p_{ij} = p; r_i \sum w_i T_i$

- maximal open:

$F2; S1 s_{ij} = 1 C_{max}$	$F3; S1 p_{ij} = p \sum U_i$
$F3; S1 p_{ij} = p; r_i C_{max}$	$F; S1 p_{ij} = 1 \sum U_i$
$F; S1 p_{ij} = 1; r_i C_{max}$	$F; S1 p_{ij} = p; s_{ij} = s; r_i \sum w_i U_i$
$F; S1 p_{ij} = p \sum w_i C_i$	$F; S1 p_{ij} = p; s_{ij} = s; r_i \sum w_i T_i$
