Flow-shop problems with transportation delays

- **maximal polynomially solvable:**

$F2\|p_{ij}=1;t_i\in\{T_1,T_2\}\|C_{max}$	Yu (1996) [5]
$F2\|t_{ik}=T\|C_{max}$	Johnson (1954) [3]
$F\|p_{ij}=1;t_i\|\sum C_i$	Brucker et al. (2004) [1]
$F\|p_{ij}=1;t_k;r_i\|\sum w_iU_i$	Single-machine problem
$F\|p_{ij}=1;t_k;r_i\|\sum w_iT_i$	Single-machine problem

- **minimal NP-hard:**

*	$F2\|p_{ij}=1;t_i\|C_{max}$	Yu (1996) [5], Yu et al. (2004) [6]
*	$F2\|r_i\|C_{max}$	Lenstra et al. (1977) [4]
*	$F2\|t_i\in\{T_1,T_2\}\|C_{max}$	Yu (1996) [5]
*	$F3\|\|C_{max}$	Garey et al. (1976) [2]
*	$F2\|\|L_{max}$	Lenstra et al. (1977) [4]
*	$F2\|\|\sum C_i$	Garey et al. (1976) [2]
*	$F2\|p_{ij}=1;t_i;r_i\|\sum C_i$	Brucker et al. (2004) [1]
*	$F2\|p_{ij}=1;t_i\|\sum w_iC_i$	Brucker et al. (2004) [1]

- **minimal open:**

$F2|p_{ij}=1;t_i\in\{T_1,T_2\};r_i|C_{max}$
$F3|p_{ij}=1;t_i\in\{T_1,T_2\}|C_{max}$
$F2|p_{ij}=1;t_i\in\{T_1,T_2\}|L_{max}$
$F2|p_{ij}=1;t_i\in\{T_1,T_2\};r_i|\sum C_i$
$F3|p_{ij}=1;t_i\in\{T_1,T_2\};r_i|\sum C_i$
$F3|p_{ij}=1;t_{ik}|\sum C_i$
$F2|p_{ij}=1;t_i\in\{T_1,T_2\}|\sum w_iC_i$
$F3|p_{ij}=1;t_i\in\{T_1,T_2\}|\sum w_iC_i$

- **maximal open:**

$F|p_{ij}=1;t_{ik}|\sum C_i$
$F|p_{ij}=1;t_i\in\{T_1,T_2\};r_i|\sum w_iU_i,\sum w_iT_i$
$F3|p_{ij}=1;t_{ik};r_i|\sum w_iU_i,\sum w_iT_i$

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